

# **Deep Learning Basics**

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## **References and Slide Credits**

- Slides from *Deep Learning for Computer Vision*, Prof. Yu-Chiang Frank Wang, National Taiwan University
- Slides from Machine Learning, Prof. Hung-Yi Lee, EE, National Taiwan University
- Slides from CE 5554 / ECE 4554: Computer Vision, Prof. J.-B. Huang, Virginia Tech
- http://cs231n.stanford.edu/syllabus.html
- Marc'Aurelio Ranzato, Tutorial in CVPR2014
- Ian Goodfellow, Yoshua Bengio, and Aaron Courville, Deep Learning
  - https://www.deeplearningbook.org/
- Bishop, Pattern Recognition and Machine Learning
- Reference papers

## Outline

- Introduction of neural network
- Go deeper
- Introduction of convolutional neural network (CNN)
- Modern CNN models

# History of Neural Network and Deep Learning [Prof. Hung-Yi Lee]

- 1958: Perceptron (linear model)
- 1969: Perceptron has limitation
- 1980s: Multi layer perceptron
  - Do not have significant difference from DNN today
- 1986: Backpropagation
  - Usually more than 3 hidden layers is not helpful
- 1989: 1 hidden layer is "good enough", why deep?
- 2006: RBM initialization (breakthrough)
- 2009: GPU
- 2011: Start to be popular in speech recognition
- 2012: win ILSVRC image competition



**Geoffrey Hinton** 

LeCun, Yann; Bengio, Yoshua; Hinton, Geoffrey, "Deep learning," Nature, 2015.

## How Powerful? Object Recognition



#### Source:

https://devblogs.nvidia.com/parallelforall/mocha-jl-deep-learning-julia/ https://blogs.nvidia.com/blog/2016/07/29/whats-difference-artificial-intelligencemachine-learning-deep-learning-ai/

### **Biological neuron and Perceptrons**



### Simple, Complex and Hypercomplex cells





David H. Hubel and Torsten Wiesel

Suggested a **hierarchy** of **feature detectors** in the visual cortex, with higher level features responding to patterns of activation in lower level cells, and propagating activation upwards to still higher level cells.

David Hubel's Eye, Brain, and Vision



#### Hubel/Wiesel Architecture and Multi-layer Neural Network



## **Hierarchical Representation Learning**

• Successive model layers learn deeper intermediate representations.



## **Recap: Linear Classification**

- Linear Classifier
  - Let's take the input image as x, and the linear classifier as W.
    We need y = Wx + b as a 10-dimensional output vector, indicating the score for each class.
  - For example, an image with 2 x 2 pixels & 3 classes of interest we need to learn a linear classifier W (plus a bias b), so that desirable outputs y = Wx + b can be expected.



### Multi-Layer Perceptron: A Nonlinear Classifier



#### Multi-Layer Perceptron: A Nonlinear Classifier (cont'd)





h() = non-linear function $[\mathbf{w}_1^{(1)}, \dots, \mathbf{w}_M^{(1)}] = 1$ st layer's  $D \times M$  weights  $\mathbf{x} = D \times 1$  raw input



 $\mathbf{z} = M \times 1$  output of layer 1  $\mathbf{w}^{(2)} = 2$ nd layer's  $M \times 1$  weight vector

#### Multi-Layer Perceptron: A Nonlinear Classifier (cont'd)



### Let's Get a Closer Look...



































#### Weight Space of a Single Neuron



#### **Training a Single Neuron**



#### **Training a Single Neuron**



#### **Training a Single Neuron**



#### objective function:

 $\begin{array}{l} G(\boldsymbol{w}) = -\sum_{n} \left[ t^{(n)} \log \mathbf{x}(\boldsymbol{z}^{(n)}; \boldsymbol{w}) + (1 - t^{n}) \log \left( 1 - \mathbf{x}(\boldsymbol{z}^{(n)}; \boldsymbol{w}) \right) \right] & \geq 0 \\ \text{surprise } -\log p(\text{outcome}) \text{ when observing } t^{(n)} \\ \text{relative entropy between } \mathbf{x}(\boldsymbol{z}^{(n)}; \boldsymbol{w}) \text{ and } t^{(n)} \end{array} \right\} \begin{array}{l} \text{encourages neuron output} \\ \text{to match training data } {}_{36} \end{array}$


#### training data

$$\{\boldsymbol{z}^{(n)}\}_{n=1}^{N} \ \{t^{(n)}\}_{n=1}^{N}$$

inputs class labels

#### objective function:

$$\begin{split} G(\boldsymbol{w}) &= -\sum_{n} \left[ t^{(n)} \log \mathbf{x}(\boldsymbol{z}^{(n)}; \boldsymbol{w}) + (1 - t^{n}) \log \left( 1 - \mathbf{x}(\boldsymbol{z}^{(n)}; \boldsymbol{w}) \right) \right] \geq 0 \\ \boldsymbol{w}^{*} &= \operatorname*{arg\,min}_{\boldsymbol{w}} G(\boldsymbol{w}) & \operatorname{choose the weights that minimise the network's surprise about the training data \\ \frac{\mathrm{d}}{\mathrm{d}\boldsymbol{w}} G(\boldsymbol{w}) &= \sum_{n} \frac{\mathrm{d}G(\boldsymbol{w})}{\mathrm{d}\boldsymbol{x}^{(n)}} \frac{\mathrm{d}\boldsymbol{x}^{(n)}}{\mathrm{d}\boldsymbol{w}} = -\sum_{n} (t^{(n)} - \boldsymbol{x}^{(n)}) \boldsymbol{z}^{(n)} = \operatorname{prediction\ error\ x\ feature} \\ \boldsymbol{w} \leftarrow \boldsymbol{w} - \eta \frac{\mathrm{d}}{\mathrm{d}\boldsymbol{w}} G(\boldsymbol{w}) & \operatorname{iteratively\ step\ down\ the\ objective\ (gradient\ points\ up\ hill)\ {}_{37} \end{split}$$















## **Overfitting and Weight Decay**



#### training data

$$\{\boldsymbol{z}^{(n)}\}_{n=1}^{N} \{t^{(n)}\}_{n=1}^{N}$$

inputs class labels

#### objective function:

$$\begin{split} G(\boldsymbol{w}) &= -\sum_{n} \left[ t^{(n)} \log \mathbf{x}(\boldsymbol{z}^{(n)}; \boldsymbol{w}) + (1 - t^{n}) \log \left( 1 - \mathbf{x}(\boldsymbol{z}^{(n)}; \boldsymbol{w}) \right) \right] \\ E(\boldsymbol{w}) &= \frac{1}{2} \sum_{i} w_{i}^{2} \quad \text{regulariser discourages the network using extreme weights} \\ \boldsymbol{w}^{*} &= \operatorname*{arg\,min}_{\boldsymbol{w}} M(\boldsymbol{w}) = \operatorname*{arg\,min}_{\boldsymbol{w}} \left[ G(\boldsymbol{w}) + \alpha E(\boldsymbol{w}) \right] \\ \frac{\mathrm{d}}{\mathrm{d}\boldsymbol{w}} M(\boldsymbol{w}) &= -\sum_{n} (t^{(n)} - \boldsymbol{x}^{(n)}) \boldsymbol{z}^{(n)} + \alpha \boldsymbol{w} \quad \text{weight decay - shrinks weights towards zero} \end{split}$$













#### Single Hidden Layer Neural Networks



## Sampling Random Neural Network Classifiers





$$x(a) = \frac{1}{1 + \exp(-a)}$$
$$a = \sum_{k=1}^{K} w_k x_k$$
$$x(a_k) = \frac{1}{1 + \exp(-a_k)}$$
$$a_k = \sum_{d=1}^{D} W_{k,d} z_d$$

#### objective function:

$$\begin{split} G(W, \boldsymbol{w}) &= -\sum_{n} \left[ t^{(n)} \log x^{(n)} + (1 - t^{n}) \log \left( 1 - x^{(n)} \right) \right] \text{ likelihood same as before} \\ E(W, \boldsymbol{w}) &= \frac{1}{2} \sum_{i} w_{i}^{2} + \frac{1}{2} \sum_{ij} W_{ij}^{2} & \text{regulariser discourages extreme weights} \\ \{W, \boldsymbol{w}^{*}\} &= \underset{W, \boldsymbol{w}}{\arg \min} M(W, \boldsymbol{w}) = \underset{W, \boldsymbol{w}}{\arg \min} \left[ G(W, \boldsymbol{w}) + \alpha E(W, \boldsymbol{w}) \right] \end{split}$$

Networks with hidden layers can be fit using gradient descent using an algorithm called back-propagation.



$$x(a) = \frac{1}{1 + \exp(-a)}$$
$$a = \sum_{k=1}^{K} w_k x_k$$
$$x(a_k) = \frac{1}{1 + \exp(-a_k)}$$
$$a_k = \sum_{d=1}^{D} W_{k,d} z$$

#### objective function:

$$\begin{split} G(W, \boldsymbol{w}) &= -\sum_{n} \left[ t^{(n)} \log x^{(n)} + (1 - t^{n}) \log \left( 1 - x^{(n)} \right) \right] \text{ likelihood same as before } \\ E(W, \boldsymbol{w}) &= \frac{1}{2} \sum_{i} w_{i}^{2} + \frac{1}{2} \sum_{ij} W_{ij}^{2} & \text{regulariser discourages extreme weights } \\ \{W, \boldsymbol{w}^{*}\} &= \operatorname*{arg\,\min}_{W, \boldsymbol{w}} M(W, \boldsymbol{w}) = \operatorname*{arg\,\min}_{W, \boldsymbol{w}} \left[ G(W, \boldsymbol{w}) + \alpha E(W, \boldsymbol{w}) \right] \\ \frac{\mathrm{d}G(W, \boldsymbol{w})}{\mathrm{d}W_{ij}} &= \sum_{n} \frac{\mathrm{d}G(W, \boldsymbol{w})}{\mathrm{d}x^{(n)}} \frac{\mathrm{d}x^{(n)}}{\mathrm{d}W_{ij}} = \sum_{n} \frac{\mathrm{d}G(W, \boldsymbol{w})}{\mathrm{d}x^{(n)}} \frac{\mathrm{d}x^{(n)}}{\mathrm{d}x^{(n)}} \frac{\mathrm{d}a^{(n)}}{\mathrm{d}x^{(n)}} \frac{\mathrm{d}a^{($$















## **Hierarchical Models with Many Layers**



# Convolutional Neural Networks (CNN): Local Connectivity



Hidden layer

Input layer



**Global** connectivity

Local connectivity

- # input units (neurons): 7
- # hidden units: 3
- Number of parameters
  - Global connectivity: 21
  - Local connectivity: 9

# Convolutional Neural Networks (CNN): Weight Sharing



Hidden layer

Input layer



#### Without weight sharing

#### With weight sharing

- # input units (neurons): 7
- # hidden units: 3
- Number of parameters
  - Without weight sharing: 9
  - With weight sharing : 3

# **CNN with Multiple Input Channels**





Single input channel



Multiple input channels



Filter weights

## **CNN with Multiple Output Maps**



Single output map





## **Generalized to 2D Cases:**

# **Fully Connected Layer**

Example: 200x200 image 40K hidden units ~2B parameters!!! - Spatial correlation is local - Waste of resources + we have not enough 33 training samples anyway.. Ranzato

Ref: Marc'Aurelio Ranzato, Tutorial in CVPR2014

#### **Generalized to 2D Cases:**

# **Locally Connected Layer**

Example: 200x200 image 40K hidden units Filter size: 10x10 4M parameters

Note: This parameterization is good when input image is registered (e.g., <sub>34</sub> face recognition). Ranzato

Ref: Marc'Aurelio Ranzato, Tutorial in CVPR2014

## **Generalized to 2D Cases:**

# **Convolutional Layer**

Share the same parameters across different locations (assuming input is stationary):

Convolutions with learned kernels



Ref: Marc'Aurelio Ranzato, Tutorial in CVPR2014

# **Convolutional Layer**



Input

Output

# **Convolutional Layer**



Input

Output


Input



Input



Input



Input



Input

# **Convolutional Layer** Learn multiple filters. E.g.: 200x200 image **100 Filters** Filter size: 10x10 **10K** parameters



Ref: Marc'Aurelio Ranzato, Tutorial in CVPR2014

### Putting them together $\rightarrow$ CNN

- Local connectivity
- Weight sharing
- Handling multiple input channels
- Handling multiple output maps



### **Convolution Layer in CNN**



• The brain/neuron view of CONV layer





It's just a neuron with local connectivity...

the result of taking a dot product between the filter and this part of the image (i.e. 5\*5\*3 = 75-dimensional dot product)

• The brain/neuron view of CONV layer



An activation map is a 28x28 sheet of neuron outputs:

- 1. Each is connected to a small region in the input
- 2. All of them share parameters

"5x5 filter" -> "5x5 receptive field for each neuron"

• The brain/neuron view of CONV layer



E.g. with 5 filters, CONV layer consists of neurons arranged in a 3D grid (28x28x5)

There will be 5 different neurons all looking at the same region in the input volume

Image input with 32 x 32 pixels convolved repeatedly with 5 x 5 x 3 filters shrinks volumes spatially (32 -> 28 -> 24 -> ...).



### Variations of Convolution

- Zero Padding
  - Output is the same size as input (doesn't shrink as the network gets deeper).



### Variations of Convolution

- Stride
  - Step size across signals



### Variations of Convolution

- Stride
  - Step size across signals



#### Nonlinearity Layer in CNN



## Nonlinearity Layer

- E.g., ReLU (Rectified Linear Unit)
  - Pixel by pixel computation of max(0, x)



#### **Receptive Field**

• For convolution with kernel size *n* x *n*, each entry in the output layer depends on a *n* x *n* receptive field in the input layer.



Each successive convolution adds n-1 to the receptive field size.
With a total of L layers, the receptive field size would be 1 + L \* (n-1).



Thus, for large images, we need many layers for each entry in output to "see" the entire input image.
Possible solution → downsample the image/feature map (see pooling layer next)

#### Pooling Layer in CNN



## **Pooling Layer**

- Makes the representations smaller and more manageable
- Operates over each activation map independently
- E.g., Max Pooling



### Pooling Layer for 2D Cases

• Reduces the spatial size and provides spatial invariance



### Fully Connected (FC) Layer in CNN



#### FC Layer

• Contains neurons that connect to the entire input volume, as in ordinary neural networks



#### FC Layer

• Contains neurons that connect to the entire input volume, as in ordinary neural networks



#### CNN



#### LeNet

- Presented by Yann LeCun during the 1990s for reading digits
- Has the elements of modern architectures



## LeNet [LeCun et al. 1998]







Gradient-based learning applied to document recognition [LeCun, Bottou, Bengio, Haffner 1998]

## **New Driving Forces**

- CPU/GPU computing
  - Personal super computer
- Internet → big data → large datasets become available

### AlexNet [Krizhevsky et al., 2012]

- Repopularized CNN by winning the ImageNet Challenge 2012
- 7 hidden layers, 650,000 neurons, 60M parameters
- Error rate of 16% vs. 26% for 2<sup>nd</sup> place.







Krizhevsky et al. "ImageNet classification with deep convolutional neural networks," NIPS, 2012.

## AlexNet



- Parameters
  - Convolution: 1.89M parameters = 7.56MB
  - Fully connected: 58.62M parameters = 234.49MB
- Computation
  - Convolution: 591M Floating MAC
  - Fully connected: 58.62M Floating MAC
  - Full-HD 30fps: 805 GFLOPS (no overlap)

#### **Deep or Not?**

• Depth of the network is critical for performance.



AlexNet: 8 Layers with 18.2% top-5 error

Removing Layer 7 reduces 16 million parameters, but only 1.1% drop in performance! Removing Layer 6 and 7 reduces 50 million parameters, but only 5.7% drop in performance Removing middle conv layers reduces 1 million parameters, but only 3% drop in performance Removing feature & conv layers produces a 33% drop in performance

## Ultra Deep Network

7.3%

http://cs231n.stanford.e du/slides/winter1516\_le cture8.pdf

8 layers



AlexNet (2012)



## Ultra Deep Network

[Prof. H.-Y. Lee]



101 layers

# VGG (2014)

- Parameters:
  - Convolution: ~14M, 56MB
  - Fully connected: ~124M, 496MB
- Computation:
  - Convolution: 15.52G Floating MAC
  - Fully connected: 123.63M Floating MAC
  - Full-HD 30fps: 19.3TFLOPS(no overlap)

image
conv-64
conv-64
maxpool
conv-128
conv-128
maxpool
conv-256
conv-256
maxpool
conv-512
conv-512
maxpool
conv-512
conv-512
maxpool
EC 4006
FC-4096
FC-4096
FC-1000
softmax

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## ResNet (2016)

• Can we just increase the #layer?



- How can we train very deep network?
  - Residual learning



method	top-5 err. (test)
VGG [41] (ILSVRC'14)	7.32
GoogLeNet [44] (ILSVRC'14)	6.66
VGG [41] (v5)	6.8
PReLU-net [13]	4.94
BN-inception [16]	4.82
ResNet (ILSVRC'15)	3.57

Ref: He, Kaiming, et al. "Deep residual learning for image recognition." *CVPR*, 2016.

## DenseNet (2017)

- Shorter connections (like ResNet) help
- Why not just connect them all?



27.5

26.5

ResNets - DenseNets-BC

4ResNet-34

ADenseNet-121
## ResNeXT (2017)

- Deeper and wider → better...what else?
  - Increase cardinality



Xie, Saining, et al. "Aggregated residual transformations for deep neural networks." CVPR, 2017.

## **Squeeze-and-Excitation Net (SENet)**

- How to improve acc. without much overhead?
  - Feature recalibration (channel attention)





	original		re-implementation			SENet		
	top-1 err.	top-5 err.	top-1 err.	top-5 err.	GFLOPs	top-1 err.	top-5 err.	GFLOPs
ResNet-50 [13]	24.7	7.8	24.80	7.48	3.86	$23.29_{(1.51)}$	$6.62_{(0.86)}$	3.87
ResNet-101 [13]	23.6	7.1	23.17	6.52	7.58	$22.38_{(0.79)}$	$6.07_{(0.45)}$	7.60
ResNet-152 [13]	23.0	6.7	22.42	6.34	11.30	$21.57_{(0.85)}$	$5.73_{(0.61)}$	11.32
ResNeXt-50 [19]	22.2	-	22.11	5.90	4.24	$21.10_{(1.01)}$	$5.49_{(0.41)}$	4.25
ResNeXt-101 [19]	21.2	5.6	21.18	5.57	7.99	$20.70_{(0.48)}$	$5.01_{(0.56)}$	8.00
VGG-16 [11]	-	-	27.02	8.81	15.47	$25.22_{(1.80)}$	$7.70_{(1.11)}$	15.48
BN-Inception [6]	25.2	7.82	25.38	7.89	2.03	$24.23_{(1.15)}$	$7.14_{(0.75)}$	2.04
Inception-ResNet-v2 [21]	$19.9^{\dagger}$	$4.9^{\dagger}$	20.37	5.21	11.75	$19.80_{(0.57)}$	$4.79_{(0.42)}$	11.76

Hu, Jie, Li Shen, and Gang Sun. "Squeeze-and-excitation networks." CVPR, 2018.

## Various Deep Learning Models...



Ref: Bianco et al., "Benchmark Analysis of Representative Deep Neural Network Architectures," arXiv:1810.00736.

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